

Potential Step and Polarography Problem Set

Turn in Problems 3, 5, & 7 by Friday, February 20, 2004

1] Solve Fick's 2nd Law of Diffusion for a spherical electrode. From B+F Chapter 5 we have:

$$\frac{\partial C_0(r,t)}{\partial t} = D_0 \left(\frac{\partial^2 C_0(r,t)}{\partial r^2} + \frac{2}{r} \frac{\partial C_0(r,t)}{\partial r} \right)$$

Consider the initial conditions of $C_0(r = r_0, t = 0) = C_0^*$ $r_0 =$ radius of electrode

Boundary conditions $\lim_{r \rightarrow \infty} C_0(r,t) = C_0^*$ & $C_0(r = r_0, t > 0) = 0$

Hint: To solve let $v = rC_0$ and rewrite F.S.L. in a liner form (in v). Use reverse substitution to find α and β Laplace constants.

$$\text{Answer: } i = nFAD_0C_0^* \left(\frac{1}{(\pi D_0 t)^{1/2}} + \frac{1}{r_0} \right)$$

2] Do problem 5.6 (1980 & 2001 editions) of B+F

3] The concentration of Fe^{3+} ($\text{Fe}^{3+} + 3e^- \rightarrow \text{Fe}(\text{Hg})$) in a sample of tap water was determined by polarography. The diffusion current in a 10 ml sample was $0.15 \mu\text{A}$. After the addition of a 0.5 mM spike of 1.00 ml to the sample the diffusion current was measured $0.30 \mu\text{A}$. What is the concentration of ferric ion in the sample? Answer = $4.17 \times 10^{-5} \text{ M}$

4] The following data were obtained from the polarographic analyses of standard Pb^{2+} solutions.

$\text{Pb}^{2+} \text{ mM}$	$i_d \text{ uA}$
0.0	1.32
0.510	5.65
1.02	10.70
2.04	19.08
3.06	27.91
4.08	36.08
5.10	45.82

Two aqueous samples from the Silver Valley area were analyzed and gave i_d of 7.75 and 40.01 uA respectively. What are the Pb^{2+} concentrations in these samples? Ans = 0.878 mM ; 4.62 mM .

5] The Hg flow rate and drop lifetimes were 2.63 mg/s and 2.88 s respectively for the problem above. What is the diffusion coefficient of Pb^{2+} ? Ans = $9.8 \times 10^{-6} \text{ cm}^2/\text{s}$

6] The following polarographic data were obtained for the reduction of a $2.00 \times 10^{-3} \text{ M Pb}^{2+}$, 0.100 KNO_3 solution and a complexing agent A. From the data below derive the formula and the formation constant of the lead complex.

[A], M	$E_{1/2}$ vs. SCE, V
0.000	-0.405
0.020	-0.473
0.060	-0.507
0.101	-0.516
0.300	-0.547
0.500	-0.558

7] We have mentioned the concept of an analytical microelectrode in lecture. This problem gets that point across. A diffusion current for the reduction of Cd^{2+} is measured as 14 μA . The solution contains 25 ml of 0.50 mM Cd^{2+} and the total analysis time was 3.4 minutes.

- Calculate the fraction of Cd^{2+} reduced per minute of i_d passage.
- What is the percentage change in Cd^{2+} concentration after the analysis?